## KULEUVEN

# Introduction to Machine Learning 

H. Blockeel

Machine Learning for Constraint Programming Summer school, Leuven, July 2023

## What is Machine Learning?

## You probably heard of it...

How would you define machine learning?


Mental Model



1. mike is wearing a pirate hat 2. jenny is in the sandbox
2. mike is kicking the soccer ball 3. mike is kicking the soc
3. jenny is angry at mike 5. mike is in the sandbox


Employee shift rostering


## Many applications...

- Recommender systems: e.g., Google, Facebook, Amazon, ... try to show you ads you might like
- Email spam filters: by observing which mails you flag as "spam", try to learn your preferences
- Natural language processing: e.g., Sentiment analysis: is this movie review mostly positive or negative?
- Vision: learn to recognize pedestrians, ...
- ... and many, many more
P. Domingos' bestseller The Master Algorithm provides an excellent account of how machine learning affects our daily life


## Definitions of machine learning?

- Tom Mitchell, 1996: Machine learning is the study of how to make programs improve their performance on certain tasks from (own) experience
- "performance" = speed, accuracy, ...
- "experience" = earlier observations
- "Improve performance" in the most general meaning: this includes learning from scratch.
- Useful (in principle) for anything that we don't know how to program computer "programs itself"
- Vision: recognizing faces, traffic signs, ...
- Game playing, e.g., AlphaGo
- Link to artificial intelligence : computer solves hard problems autonomously


## Machine learning vs. other AI

- In machine learning, the key is data
- Examples of questions \& their answer
- Observations of earlier attempts to solve some problem
- Machine learning makes use of inductive inference: reasoning from specific to general
- In statistics: sample $\rightarrow$ population
- In philosophy of science: concrete observations $\rightarrow$ general theory
- In machine learning: observations $\rightarrow$ any situation
- This aspect of machine learning links it to data mining, data analysis, statistics, ...


## Machine learning and AI

- Many misconceptions about machine learning these days
- In the latest 15 years or so, "Deep Learning" has received a lot of attention: it revolutionized computer vision, speech recognition, natural language processing
- Avalanche of new researchers drawn to the field, without knowledge of the broader field of AI, or history of ML ("AI = ML = deep learning")
- See, e.g., A. Darwiche, https://www.youtube.com/watch?v=UTzCwCic-Do (also published in Communications of the ACM, October 2018)



## Machine learning and Al

- There is still progress on all fronts, deep learning is just one of them
- This course reflects that viewpoint
- (schema below is incomplete, just serves to illustrate complexity of scientific impact)



## The machine learning landscape

Automata
Neural networks

## Recommender

systems
Deep learning
Clustering

Statistical relational learning

Nearest neighbors
Decision trees

Convex
optimization

Support vector machines

Natural
language
Regression processing
Support vector
machines

|  | Natural <br> language <br> Regression |
| :---: | :---: |
|  | Nearest neighbors |

Rule learners
Classification

Matrix factorization

Probabilistic graphical models

Transfer learning
Vision

Greedy search

Reinforcement learning
Speech

Bayesian learning

## Basic concepts and terminology

## Machine learning

- ML in its typical form:
- Input = dataset
- Output = some kind of model
- ML in its most general form:
- input = knowledge
- output = a more general form of knowledge
- Learning = inferring general knowledge from more specific knowledge (observations
$\rightarrow$ model) $=$ inductive inference
- Learning methods are often categorized according to the format of the input and output, and according to the goal of the learning process (but there are many more dimensions along which they can be categorized)


## A typical task

- Given examples of pictures + label (saying what's on the picture), infer a procedure that will allow you to correctly label new pictures
- E.g.: learn to classify fish as "salmon" or "sea bass"



## A generic approach

- Find informative features (here: lightness, width)
- Find a line/curve/hyperplane/... in this feature space that separates the classes

> In this case rather than a simple threshold we must
> find a curve in the plane that separates salmons from
> sea basses





## Predictive versus descriptive

- Predictive learning : learn a model that can predict a particular property / attribute / variable from inputs
- Many tasks are special cases of predictive learning
- E.g., face recognition: given a picture of a face, say who it is
- E.g., spam filtering: given an email, say whether it's spam or not

| Name of task | Learns a model that can ... |
| :---: | :--- |
| Concept learning / <br> Binary classification | Distinguish instances of class C from other instances |
| Classification | Assign a class $C$ (from a given set of classes) to an instance |
| Regression | Assign a numerical value to an instance |
| Multi-label classification | Assign a set of labels (from a given set) to an instance |
| Multivariate regression | Assign a vector of numbers to an instance |
| Multi-target prediction | Assign a vector of values (numerical, categorical) to an instance |
| Ranking | Assign $\leq$ or > to a pair of instances |

## Predictive versus descriptive

- Descriptive learning : given a data set, describe certain patterns in the dataset (or in the population it is drawn from)
- E.g., analyzing large databases:
- "Bank X always refuses loans to people who earn less than 1200 euros per month"
- " $99.7 \%$ of all pregnant patients in this hospital are female"
- "At supermarket $X$, people who buy cheese are twice as likely to also buy wine"


## Function learning

- Task : learn a function $X \rightarrow Y$ that fits the given data (with $X$ and $Y$ sets of variables that occur in the data)
- Such a function will obviously be useful for predicting Y from X
- May also be descriptive, if we can understand the function
- Often, some family of functions F is given, and we need to estimate the parameters of the function $f$ in $F$ that best fits the data
- e.g., linear regression : determine $a$ and $b$ such that $y=a x+b$ fits the data as well as possible
- What does "fit the data" mean? Measured by a so-called loss function
- e.g., quadratic loss: $\sum_{(x, y) \in D}(f(x)-y)^{2} \quad$ with $f$ the learned function and

D the dataset

## Distribution learning

- Task: given a data set drawn from a distribution, estimate this distribution
- Often made distinction: parametric vs. non-parametric
- Parametric: a family of distributions is given (e.g., "Gaussian"), we only need to estimate the parameters of the target distribution
- Non-parametric: no specific family is assumed
- Often made distinction: generative vs. discriminative
- Generative: learn the joint probability distribution (JPD) over all variables (once you have that, you can generate new instances by random sampling from it)
- Discriminative: learn a conditional probability distribution of Y given $X$, for some given set of variables $X$ (called input variables) and $Y$ (called target variables)


Non-parametric


## These categorizations are somewhat

fuzzy...

- A descriptive pattern may be useful for prediction
- "Bank X always refuses loans to people who earn less than 1200 euros per month" (description)
- Bob earns 1100 euros per month => Bank $X$ will not give him a loan
- While functions are directly useful for prediction, a probability distribution can be used just as well
- Given known information $X$, predict as value for $Y$, the value with the highest conditional probability given X


## Parametric vs. non-parametric

- Parametric: a family of functions (or distributions, or ...) is given, and each function is uniquely defined by the values of a fixed set of parameters
- e.g. (function learning): linear regression
- e.g. (distribution learning): fitting a gaussian
- Non-parametric: no specific family of functions is assumed
- Typically, we are searching a space that contains models with varying structure, rather than just different parameter values
- This often requires searching a discrete space
- E.g.: decision trees, rules, .... (see later)


## Link with "explainable AI"

- Explainable AI (XAI) refers to the study of AI systems that can explain their decisions / whose decisions we can understand
- Two different levels here:
- We understand the (learned) model used for decision making [global]
- We understand the individual decision [local]
- E.g. "I could not get a loan because I earn too little": we can understand this decision even if we don't know the whole decision process the bank uses
- A learned model that is not straightforward to interpret, is called a blackbox model
- Machine learning poses additional challenges for XAI, as it often learns black-box models


## Responsible AI : challenges

- Privacy-preserving data analysis
- We need lots of data to learn from; this may include personal data
- How can we guarantee that the analysis of these data will not violate the privacy of the people whose data this is?
- Generally, when data is collected, consent is needed for a specific purpose, and data must be used solely for that purpose - how can we guarantee it won't be abused?
- Learning "safe" models : models that will not violate certain constraints that are imposed (including constraints on bias, discrimination, privacy, ...)


## Predictive learning

- A very large part of machine learning focuses on predictive learning
- The prediction task, in general:
- Given: a description of some instance
- Predict: some property of interest (the "target")
- Examples:
- classify emails as spam / non-spam
- classify fish as salmon / bass
- forecast tomorrow's weather based on today's measurements
- How? By analogy to cases seen before


## Training \& prediction sets

- Training set: a set of examples, instance descriptions that include the target property (a.k.a. labeled instances)
- Prediction set: a set of instance descriptions that do not include the target property ("unlabeled" instances)
- Prediction task : predict the labels of the unlabeled instances



## Inductive vs. transductive learning

We can consider as outcome of the learning process, either

- the predictions themselves: transductive learning
- or: a function that can predict the label of any unlabeled instance: inductive learning


Transduction: outcome=predictions


Induction: outcome = function
for making predictions

## Inductive vs. transductive learning

We can consider as outcome of the learning process, either

- the predictions themselves: transductive learning
- or: a function that can predict the label of any unlabeled instance: inductive learning


Transduction: outcome=predictions


Induction: outcome = function
for making predictions

## Inductive vs. transductive learning

We can consider as outcome of the learning process, either

- the predictions themselves: transductive learning
- or: a function that can predict the label of any unlabeled instance: inductive learning


Transduction: outcome=predictions


Induction: outcome = function
for making predictions

## Interpretable vs. black-box

The predictive function or model learned from the data may be represented in a format that we can easily interpret, or not

Non-interpretable models are also called black-box models

In some cases, it is crucial that predictions can be explained (e.g.: bank deciding whether to give you a loan)

Note difference between explaining a model and explaining a prediction

## Overfitting and underfitting

- "Occam's razor": among equally accurate models, choose the simpler one
- Trade-off: explain data vs. simplicity
- Both overfitting and underfitting are harmful



## Levels of supervision

- Supervised learning: learning a (predictive) model from labeled instances (as in cats \& dogs example)
- Unsupervised learning: learning a model from unlabeled instances
- such models are usually not directly predictive (without any information on what to predict, how could you learn from that?)
- still useful indirectly, or for non-predictive tasks: see later
- Semi-supervised learning: learn a predictive model from a few labeled and many unlabeled examples


## Semi-supervised learning

- How can unlabeled examples help learn a better model?

$$
+\quad-
$$

$$
\ddagger
$$

This illustration:

- 2 classes, called + and -
- Representing instances in a 2-dimensional space


## Semi-supervised learning

- How can unlabeled examples help learn a better model?



## Semi-supervised learning

- How can unlabeled examples help learn a better model?



## Unsupervised learning

- Can you see three classes here?
- Even though we don't know the names of the classes, we still see some structure (clusters) that we could use to predict which class a new instance belongs to
- Identifying this structure is called clustering
- From a predictive point of view, this is unsupervised learning



## PU-learning

- PU-learning is a special case of semi-supervised learning
- PU stands for "positive / unlabeled"
- All the labeled examples belong to one class (called the "positive" class)

"Mike is kicking the ball"
Learning the meaning of "kicking the ball" requires PU-learning because:
When Mike kicks the ball, the sentence may mention this, or not. When Mike does not kick the ball, it is never mentioned that he does not.



## Weakly supervised learning

- Weakly supervised learning is a generalized form of semi-supervised learning
- Semi-supervised: for a single instance, we either know its label or we do not
- Weakly supervised: we may have partial information about a label
- e.g., it is certainly a member of a given set (= superset learning)
- e.g., at least one instance among a given set of instances has the label, but we do not know which one (= multi-instance learning)
- e.g., we know two instances have the same label, but we don't know which one it is (= constraint-based clustering)
- ... or a Lamborghini"

"There's a Lamborghini in this picture"


## Relationship between different supervision settings



## Reinforcement learning

- Sometimes viewed as another form of supervision, but it's different in more ways than just that
- The setting:
- an agent can be in any of a number of states
- it can take actions that change its state and may give some reward
- it wants to maximize its rewards in the long run
- How should it behave?
- Formally, given a state space $S$, transition function $\delta: S \times A \rightarrow S$, reward function
$r: S \times A \rightarrow \mathbb{R}$, and discount factor $\gamma \in[0,1]$, find a policy that maximizes $\sum_{i=0}^{\infty} \gamma^{i} r\left(s_{i}, \pi\left(s_{i}\right)\right)$ where $s_{i+1}=\delta\left(s_{i}, \pi\left(s_{i}\right)\right)$
- $\delta$ and $r$ are initially unknown to the agent
- The agent generates its own training data (through exploration)


## Illustration: Q-learning

- Agent updates a function $Q(s, a)$ that ultimately converges to $r(s, a)+\sum_{i=1}^{\infty} \gamma^{i} r\left(s_{i}, \pi^{*}\left(s_{i}\right)\right)$ where $\pi^{*}$ is the optimal policy
- ... so that choosing the $a$ that maximizes $Q(s, a)$ is by definition optimal (hence, defines $\pi^{*}$ )

1: Initialise $Q$ randomly;
2: Initialize $s$;
3: while (true) do
4: $\quad$ Choose an action $a$;
5: $\quad$ Execute $a$ and observe $r$ and $s$;;
6: $\quad Q(s, a):=r+\gamma \max _{a^{\prime}} Q\left(s^{\prime}, a^{\prime}\right)$;
7: $\quad s:=s$;
8:end while

## $\mathrm{Q}(\mathrm{s}, \mathrm{a}) \leftarrow 0.0+0.9 \times 1.0 \mathrm{Q}\left(\mathrm{s}^{\prime}, \mathrm{a}^{\prime}\right)$

Right

| 0 | 0 | 0 | 0 |
| :--- | :--- | :--- | :--- |
| 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 |

## Some comments

- In the illustration, the agent updated a table-based representation of $Q(s, a)$
- We can use that table as feedback to learn what kind of actions work well in what kind of states. That is, we learn a model of the $Q$ function. This is model-based reinforcement learning
- We assumed a deterministic environment, but RL is often formulated in a probabilistic environment: Markov Decision Processes (MDP)
- We here assumed random exploration, but more clever versions exist (gradually increasing exploration of more promising parts of the state-action space)


## Encoding data

- An unsupervised learning task: learn functions $f: \mathscr{X} \rightarrow \mathbb{R}^{k}$ and $g: \mathbb{R} \rightarrow \mathscr{X}$ such that $g \circ f$ is the identity function
- When $\mathscr{X}=\mathbb{R}^{m}$, typically $k \ll m$ : dimensionality reduction
- When $\mathscr{X}$ is not a vector space, $f$ is called an embedding
- $f$ is called the encoder and $g$ the decoder
- Encoding can be useful for understanding the structure of the input space



## Probabilistic encoders

- A "standard" encoder learns $f: \mathscr{X} \rightarrow \mathbb{R}^{k}$ and $g: \mathbb{R} \rightarrow \mathscr{X}$ such that $g \circ f$ is the identity function
- We can also consider probabilistic encoders, which are trained to reconstruct the input distribution over $\mathscr{X}$ but not individual cases
- That is: we learn $f: \mathscr{X} \rightarrow \mathbb{R}^{k}$ and $g: \mathbb{R} \rightarrow \mathscr{X}$ such that the distribution of $g \circ f(x)$ is equal to the distribution of $x$
- The distribution of $f(x)$ is called the latent distribution
- This is useful for training, e.g., generative models


Format of input data

## Format of input data

- Input is often assumed to be a set of instances that are all described using the same variables (features, attributes)
- The data are "i.i.d.": "independent and identically distributed"
- The training set can be seen as a random sample from one distribution
- The training set can be shown as a table (instances x variables) : tabular data
- This is also called the standard setting
- There are other formats: instances can be
- nodes in a graph
- whole graphs
- elements of a sequence
- ...


## Format of input data: tabular

Training set

| Sepal <br> length | Sepal <br> widith | Petal <br> length | Petal <br> width | Class |
| ---: | ---: | ---: | ---: | ---: | ---: |
| 5.1 | 3.5 | 1.4 | 0.2 | Setosa |
| 4.9 | 3.0 | 1.4 | 0.2 | Setosa |
| 7.0 | 3.2 | 4.7 | 1.4 | Versicolor |
| 6.3 | 3.3 | 6.0 | 2.5 | Virginica |

Prediction set

| Sepal <br> length | Sepal <br> widith | Petal <br> length | Petal <br> width | Class |
| ---: | ---: | ---: | ---: | ---: |
| 4.8 | 3.2 | 1.3 | 0.3 | $?$ |
| 7.1 | 3.3 | 5.2 | 1.7 | $?$ |

## Format of input data: sequences

- Learning from sequences:
- 1 prediction per sequence?
- 1 prediction per element?
- 1 element in sequence can be ...
- A number (e.g., time series)
- A symbol (e.g., strings)
- A tuple
- A more complex structure

abababab: +<br>aabbaabb: -

## Format of input data: trees

- 1 prediction per tree / per node in the tree
- Nodes can be ...
- Unlabeled
- Labeled with symbols (e.g., HTML/XML structures)
E.g.: this tree indicates as "positive" a text field preceded by Address: inside a list (<li>) context

"Adress:"-


## Format of input data: graph

- Example: Social network
- Target value known for some nodes, not for others
- Predict node label
- Predict edge
- Predict edge label
- Use network structure for
 these predictions


## Format of input data: raw data

- "Raw" data are in a format that seems simple (e.g., a vector of numbers), but components $\neq$ meaningful features
- Example: photo (vector of pixels)
- Raw data often need to be processed in a non-trivial way to obtain meaningful features; on the basis of these features, a function can be learned
- This is what deep learning excels at

(Image: Nielsen, 2017, Neural networks and deep learning)


## Format of input data: knowledge

- "Knowledge" can consist of facts, rules, definitions, ....
- We can represent knowledge about some domain in a knowledge representation language (such languages are often based on logic)

| $\operatorname{atm}(\mathrm{m} 1, \mathrm{a} 1, \mathrm{o}, 2,3.43,-3.11,0.04)$. | $\cdots$ |
| :---: | :---: |
| $\operatorname{atm}(\mathrm{ml}, \mathrm{a} 2, \mathrm{c}, 2,6.03,-1.77,0.67)$. | $\begin{aligned} & \text { hacc(M,A):- } \left.\operatorname{atm}\left(\mathrm{M}, \mathrm{~A}, \mathrm{o}, 2,,_{-},\right)_{-}\right) . \\ & \operatorname{hacc}(\mathrm{M}, \mathrm{~A}):-\operatorname{atm}(\mathrm{M}, \mathrm{~A}, \mathrm{o}, 3,-,,-) . \end{aligned}$ |
| bond(m1, a2, a3,2). |  |
| bond(m1, $\mathrm{a} 5, \mathrm{a6,1}$ ). | $\operatorname{hacc}(\mathrm{M}, \mathrm{A}):-\mathrm{atm}(\mathrm{M}, \mathrm{A}, \mathrm{n}, \mathrm{ar},-$, , $)$. |
| bond(m1, a6, a7,du). | $\begin{aligned} & \text { zincsite(M,A):- } \\ & \quad \operatorname{atm}(\mathrm{M}, \mathrm{~A}, \mathrm{du},,-,-,-) . \\ & \text { hdonor(M,A) :- } \end{aligned}$ |
|  |  |
|  | $\begin{aligned} & \operatorname{atm}(\mathrm{M}, \mathrm{~A}, \mathrm{~h},-,-,=,), \\ & \text { not(carbon_bond(M,A)), !. } \end{aligned}$ |
|  | $\ldots$ |



## Data preprocessing

- Data may not be in a format that your learner can handle
- Data wrangling: bring it into the right format
- Even if it's in a format you learner can handle (e.g., tabular), the features it contains may not be very informative, or there may be very few relevant features among many irrelevant ones.
- E.g.: individual pixels in an image are usually not very informative
- Feature selection: select among many input features the most informative ones
- Feature construction: construct new features, derived from the given ones


## What learning method to use?

- Which learners are suitable for your problem, depends strongly (but not solely!) on the structure of the input data
- Many learners use the standard format
- A set of instances, where each instance is described by a fixed set of attributes (a.k.a. features, variables)
- also called attribute-value format or tabular format
- Other learners handle input knowledge with a more complex structure (sequences, graphs, ...) or raw data
- Different learners have a different inductive bias


# Output formats, methods (overview) 

## Output formats

- The output of a learning system is a model
- Many different types of model exist
- The learning algorithm or method is strongly linked to the type of model
- High-level overviews of machine learning methods often categorize them along this axis


## Different views of the landscape

Domingos: "five tribes"

- Symbolists
- Connectionists
- Evolutionaries
- Bayesians
- Analogizers

Flach:
"three types of models"

- Probabilistic
- Geometric
- Logical


Bishop:
"Ultimately, everything is Bayesian"

- Bayes



## Parametrized functions

- Typically, a certain format for the functions is provided; e.g.: linear functions of the inputs
- Within this set, we look for the parameter values that best fit the data
- Standard example: linear regression


```
\(y=a x+b\)
width \(=0.416^{*}\) length -0.363
```


## Conjunctive concepts

- A conjunctive concept is expressed as a set of conditions, all of which must be true
- "x has class C if and only if <condition1> and <condition2> and ... and <condition k>"
- E.g.: accept application for mortgage if and only if : salary $\geq 3$ * monthly payback and no other mortgage running


## Rule sets

- A rule set is a set of rules of the form "if ... then ..." or "if ... then ... else ..."
- Example: definition of leap years

$$
\begin{aligned}
& \text { Examples of leap years: } \\
& 1900,1992,2004, \ldots \\
& \text { Examples of non-leap years: } \\
& 1993,2000,2011,2018, \ldots
\end{aligned}
$$

Output


## Decision trees

- A decision tree represents a stepwise procedure to arrive at some decision

Is today a good day to play tennis?


## Instance-based learning (a.k.a. "nearest neighbor methods")

- The "model" is simply the data set itself
- Predictions for new cases are made by comparing it to earlier observed cases
- If it's similar for observed features, it's probably also similar for unobserved (to be predicted) features




## Probabilistic graphical models

- A PGM represents a (high-dimensional) joint distribution over multiple variables as a product of (low-dimensional) factors
- Different type of PGMs: Bayesian networks, Markov networks, factor graphs, ...

Example: Bayesian network

$f(a, b, c, d, e)=f_{1}(a) \cdot f_{2}(b) \cdot f_{3}(a, b, c) \cdot f_{4}(c, d) \cdot f_{5}(c, e)$
$P(A, B, C, D, E)=P(A) \cdot P(B) \cdot P(C \mid A, B) \cdot P(D \mid C) \cdot P(E \mid C)$

## Neural networks

- A neural network is a complex structure of neurons, each of which aggregate multiple input signals into a single output signal



## Advanced NN architectures

- The network we just saw just stacked a few layers of neurons on top of each other
- Much more advanced architectures exist, which serve a specific purpose
- e.g. convolutional networks scan a picture for patterns (the scanning is hard-wired, the patterns to look for are learned)
- LSTMs process sequences of data sequentially, and have memory cells that allow them to store info for re-use later on (the memory is hard-wired, what to remember when is learned)
- Transformer models process sets/sequences by enriching their elements with context info ("attention") and processing everything simultaneously, not sequentially


## Illustration: convolutional step

- In this example, the "map" essentially lights up in those positions where a sub-image similar to the kernel was found
- Note: convolution layers are translation-invariant (sub-image is found regardless of position in the picture) but not rotation- or scale-invariant: need to train on rotated / scaled versions separately



## Illustration: Sutskever et al.'s "Sequence to sequence learning with neural networks" (2014)

- Example instance: ik speel piano <eos> I play the piano <eos>



## KULEUVEN

## Illustration: Transformer

- Figure to the right (from Vaswani et al.) shows the architecture of the full transformer model
- Left = encoder, right = decoder
- The link between encoder \& decoder is an attention layer that works similar to Bahdanau's attention
- The input and output self-attention layers (with feedforward NN stacked on top) replace the RNNs
- The decoder uses masked attention: it is not allowed to look at words that will be generated later
- The positional encoding added to words uses periodic functions (sin/cos) with various periods
- More details in Vaswani et al. (incl. code \& appendices)


Figure 1: The Transformer - model architecture.

## Illustration: BERT

- Input = a single sentence, or a pair of sentences
- Model is trained on multiple different pre-training tasks
- "Masked LM": mask some words, model must predict them
- "Next sentence prediction": labeled pairs of sentences (next, not-next)

Illustration from
Devlin et al.

| Input | [CLS] | my | dog | is | cute | [SEP] | he | likes | play | \#\#ing | [SEP] |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Token Embeddings | $\mathrm{E}_{[\mid C L S]}$ | $\mathrm{E}_{\mathrm{my}}$ | $\mathrm{E}_{\text {dog }}$ | $\mathrm{E}_{\text {is }}$ | $\mathrm{E}_{\text {cute }}$ | $\mathrm{E}_{\text {[SEP] }}$ | $\mathrm{E}_{\text {he }}$ | $\mathrm{E}_{\text {likes }}$ | $\mathrm{E}_{\text {play }}$ | $\mathrm{E}_{* \pm \text { ing }}$ | $\mathrm{E}_{\text {[SEP] }}$ |
|  | + | + | + | + | + | + | + | + | + | + | + |
| Segment Embeddings | $E_{\text {A }}$ | $\mathrm{E}_{\mathrm{A}}$ | $\mathrm{E}_{\mathrm{A}}$ | $\mathrm{E}_{\mathrm{A}}$ | $\mathrm{E}_{\text {A }}$ | $\mathrm{E}_{\mathrm{A}}$ | $E_{B}$ | $E_{B}$ | $E_{B}$ | $\mathrm{E}_{B}$ | $\mathrm{E}_{\mathrm{B}}$ |
|  | + | + | + | + | + | + | + | + | + | + | + |
| Position Embeddings | $\mathrm{E}_{0}$ | $\mathrm{E}_{1}$ | $\mathrm{E}_{2}$ | $\mathrm{E}_{3}$ | $\mathrm{E}_{4}$ | $\mathrm{E}_{5}$ | $\mathrm{E}_{6}$ | $\mathrm{E}_{7}$ | $\mathrm{E}_{8}$ | $\mathrm{E}_{9}$ | $\mathrm{E}_{10}$ |

Figure 2: BERT input representation. The input embeddings are the sum of the token embeddings, the segmentation embeddings and the position embeddings.

## Search methods

- How do we find the most suitable model?
- Sometimes, there is a closed form solution (e.g., linear regression)
- If not, we typically need to search some hypothesis space
- Two very different types of spaces, each with their own search methods :
- Discrete spaces (methods: hill-climbing, best-first, ...)
- Continuous spaces (methods: gradient descent, ...)
- Typically:
- Model structure not fixed in advanced => discrete
- Fixed model structure, tune numerical parameters => continuous

Example: gradient descent in a continuous space


$$
(a, b) \text { represents } y=a x+b
$$

Input/output space
Parameter space

## Example: Version Spaces

- The goal: identify a conjunctive concept from data
- = a symbolic description of some concept, consisting of a conjunction of conditions
- More specific: given a hypothesis space H (all possible descriptions), return all concepts in H that are consistent with the data. This set is called the Version Space. When the version space is a singleton, the concept has been identified
- The algorithm called Candidate Elimination does this by exploiting a generality ordering over H , and returning only the most general and most specific hypotheses in H that are consistent with the data (the "borders" of H)
- This involves an exhaustive search in a discrete space


## Candidate Elimination: illustration

- A company produces intelligent robots. Some robots misbehave. We suspect that one particular combination of features is the cause for this misbehavior.
- For ease of discussion, we here assume robots have four relevant characteristics:
- Color : B R M
- Body shape : S T
- =Legs/wheels: L W
- \#"eyes": 12

- 



OO
(0) 00

- Find the combination that misbehaves


## Candidate Elimination: illustration

- We will represent a hypothesis as a tuple <color, body, legs, eyes> where color $=B, R, M$ or ? (? means "any color") etc.
- Hypothesis space: $\{B, R, M, ?\} \times\{S, T, ?\} \times\{L, W, ?\} \times\{1,2, ?\}$
- Let $S(h)$ be the set of robots characterized by a hypothesis $h$
- Hypothesis $h_{1}$ is more general than $h_{2}$ if and only if $S\left(h_{2}\right) \subseteq S\left(h_{1}\right)$
- Most general hypothesis is ...
censored
- Most specific hypothesis is


## Search space is a lattice



BSL? BSW? BTL? BTW?


BSL1 BSL2 BSW1 BSW2 BTL1 BTL2 BTW1 BTW2

## Candidate Elimination



## Candidate Elimination

Observation 2:
Does not misbehave


MTL2 MTW1 MTW2

KULEUVEN

## Candidate Elimination



## Candidate Elimination



## Candidate Elimination

- The candidate elimination algorithm illustrates
- Search in a discrete hypothesis space (with lattice structure)
- Search for all solutions, rather than just one, in an efficient manner
- Importance of generality ordering
- Some obvious disadvantages:
- Not robust to noise: result = set of hypotheses consistent with all data; 1 erroneous data point $\rightarrow$ set may be empty!
- Only conjunctive concepts : strong limitation


## 1 solution vs. set of solutions

- Predictive learning usually finds 1 model
- Candidate Elimination is an example of a method that returns a set of solutions
- Other examples of this setting:
- Find all patterns (in some given pattern space) that satisfy some given criteria
- association rules
- constraints formulated in first order logic


## Association rules

- Prototypical example from "market basket analysis": "people who buy A,B,C also buy D,E"
- General format: if $a_{1}, a_{2}, \ldots, a_{n}$ then $a_{n+1}, a_{n+2}, \ldots, a_{n+m}$
- Rule "If <this> then <that>" is characterized by
- Support: \% of all clients that buy <this>
- Low support means: of marginal importance
- Confidence: \% of buyers of <this> that also buy <that>
- Confidence need not be close to $100 \%$
- Any increase over normal level indicates an association
- Task: find the set of all association rules with support \& confidence above a chosen threshold

| Client | cheese | bread | butter | wine | jam | ham |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 1 | yes | yes | yes | yes | no | yes |
| 2 | yes | no | yes | no | no | no |
| 3 | no | yes | yes | no | no | yes |
| $\ldots$ | $\ldots$ | $\ldots$ | $\ldots$ | $\ldots$ | $\ldots$ | $\ldots$ |

IF bread \& butter THEN cheese confidence: 50\% support: 5\%

## Illustration: Learning constraints in first order logic

Prolog dataset / knowledge base:

> male(homer). male(bart). female(marge). female(lisa). father(homer,lisa). father(homer,bart). mother(marge, lisa). mother(marge,bart). parent(homer,lisa).

Knowledge discovered:
false :- male $(\mathrm{X})$, female $(\mathrm{X})$. female $(\mathrm{X}):-$ mother $(\mathrm{X}, \mathrm{Y})$. male $(\mathrm{X}):$ :- father $(\mathrm{X}, \mathrm{Y})$. parent(X,Y) :- father(X,Y).
$\operatorname{parent}(\mathrm{X}, \mathrm{Y}):-\operatorname{mother}(\mathrm{X}, \mathrm{Y})$.

## Imposing semantic constraints on learned models

- Consider AI systems that make use of learned models
- We may want to impose (symbolic) constraints on their behavior (fairness, safety, ...)
- E.g. autonomous driving: observe speed limits
- E.g. bank loans: monotonicity constraints
- Different ways of doing this:
- Fix model predictions when they violate a constraint
- Use a model for which you can verify the constraints (model verification)
- Use a learner that cannot return a model that violates the constraints - model certification

$$
(x, f(x)) \vDash C
$$

$$
\forall D: f=\operatorname{Learner}(D) \Longrightarrow f \vDash C
$$

$$
\forall x:(x, f(x)) \vDash C
$$

## Formulation as a MaxSMT(NRA) problem

- Given a parametrized class of functions $f_{\theta}$, a set of hard semantic constraints $\mathscr{C}=\left\{C_{1}, \ldots C_{k}\right\}$, and a set of soft "goodness of fit" constraints $\mathscr{F}=\left\{F_{1}, \ldots F_{n}\right\}$, find a $\theta$ such that (1) $f_{\theta} \vDash C_{i}$ for all $i$ and
(2) $f_{\theta} \vDash F_{i}$ for a maximal number of $i$
- Typically, one $C_{i}$ is, e.g., of the form $\forall x \in \mathscr{X}:\left(\boldsymbol{x}, f_{\theta}(\boldsymbol{x})\right) \vDash \ldots$ : "universal constraint" (quantified over domain)
- "Goodness of fit" constraints depend on the type of learning problem, e..g,. For regression: $\left|\mid f\left(\boldsymbol{x}_{i}\right)-y_{i} \|_{2}<\varepsilon_{j}\right.$ for all $\left(\boldsymbol{x}_{i}, y_{i}\right) \in T$ with $\varepsilon_{1}<\varepsilon_{2}<\ldots<\varepsilon_{k}$ given and $T$ the training set
- Note: soft constraints express goodness of fit on $T$, hard constraints express domain constraints over $\mathscr{X}$
- MaxSMT(NRA) reasons about the real-valued parameters to ensure $f_{\theta}$ meets all hard constraints
- Practically feasible? Not without changes - but some approaches developed for linear models and ReLU-based neural networks


## End of this introduction

- Questions? Feel free to come talk to me when I'm around

